

2025

( FYUGP )

( 2nd Semester )

ECONOMICS

( MAJOR )

Paper : EC2.CC4

( **Mathematical Methods for Economics—II** )

Full Marks : 75

Pass Marks : 40%

Time : 3 hours

*The figures in the margin indicate full marks  
for the questions*

Answer **five** questions, taking **one** from each Unit

UNIT—1

1. (a) Define singular and non-singular matrix. Give example. 4

(b) If

$$A = \begin{bmatrix} 3 & 2 & 0 \\ 4 & 1 & 3 \\ 2 & 2 & 3 \end{bmatrix} \text{ and } B = \begin{bmatrix} 2 & 1 & 2 \\ 4 & 0 & 1 \\ 2 & 2 & 5 \end{bmatrix}$$

Find  $AB$ .

5

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- (c) Solve the following equation system by Cramer's rule :

$$2x + y + 3z = 15$$

$$x - 2y + 5z = 13$$

$$4x + 3y - z = 11$$

6

2. What is determinants? Explain the properties of determinants with example.

3+12=15

UNIT—2

3. (a) Find the all second-order partial derivatives of the following function : 8

$$Y = 4x_1x_2 + x_1^3 + 2x_2^2$$

- (b) A consumer consumes two commodities  $x_1$  and  $x_2$  and the utility function is given by

$$U = x_1^2 + 3x_1x_2 + 5x_2$$

Find out marginal utilities of  $x_1$  and  $x_2$ . 7

4. (a) Find the extreme value of the following function and determine whether they are maxima or minima : 8

$$Y = 5x_1^2 + 2x_2^2 - 2x_1x_2 - 15x_1 - 6x_2$$

- (b) Cobb-Douglas production function is given as  $Q = AK^\alpha L^\beta$ , where  $\alpha + \beta = 1$ , and  $L$  = labour,  $K$  = capital,  $Q$  = output and  $A$ ,  $\alpha$  and  $\beta$  are constant. Find marginal productivity of  $L$  and  $K$ . 7

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UNIT—3

5. What is Lagrange multiplier? Find the extreme value of the following function :

$$3+12=15$$

$$Y = x_1^2 + x_1x_2 + \frac{3}{2}x_2^2$$

subject to

$$x_1 + 2x_2 = 14$$

6. A monopolist discriminates in prices between two markets I and II and the price equations are given by—

$$P_1 = 60 - 4Q_1$$

$$P_2 = 42 - 3Q_2$$

where  $Q_1$  and  $Q_2$  are the outputs of markets I and II and  $Q = Q_1 + Q_2$ . The total cost (TC) =  $50 + 12Q$ . Find—

- (a) profit maximising output and prices;  
(b) maximum profit;  
(c) elasticity of demand of the markets I and II. 7+3+5=15

UNIT—4

7. Explain the inventory control technique in economics.

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8. (a) In a perfectly competitive market the total revenue ( $TR$ ) and total cost ( $TC$ ) of a firm are given by

$$TR = 20Q$$

$$TC = Q^2 + 4Q + 20$$

Find profit maximizing output ( $Q$ ). 7

- (b) A monopolist has the following total revenue and total cost functions :

$$TR = 30q - q^2$$

$$TC = q^3 - 15q^2 + 10q + 100$$

Find—

(i) profit maximizing output ( $q$ );

(ii) maximum profit. 8

#### UNIT—5

9. (a) What is differential equation? Explain the economic implications of differential equation. 2+8=10

(b) Solve :  $\frac{dy}{dx} + 2xy = 2x$  5

10. Solve the following difference equations : 5×3=15

(a)  $y_t - 2y_{t-1} = 3$  with  $y_0 = 2$

(b)  $y_{t-1} - y_t = 10$  with  $y_0 = 5$

(c)  $y_{t+1} - 5y_t = 12$  with  $y_0 = 10$

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